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Inverse Propensity Score Weights or IPTWs



- Describe Different Types of Treatment Effects
 - Average Treatment Effect
 - Average Treatment Effect among Treated
 - Average Treatment Effect among Untreated
- Introduce different Weights using Propensity Score





FUNDAMENTAL PROBLEM OF CAUSAL INFERENCE

Cannot Observe...

The same person under both conditions





Average Effects

- Effects vary from individual to individual
- Average effect tells us...

"the effect for a person--at random-- from our group."

How do we get this "average effect"?

Compare average outcomes





Average Effects

- One state: the group **receives** the Full Day Kindergarten
- One state: the group does not receive the Full Day Kindergarten
- Difference in average outcomes between the two is the average effect of Full Day Kindergarten





FUNDAMENTAL PROBLEM OF CAUSAL INFERENCE CANNOT OBSERVE GROUP under BOTH STATES

- Groups that we can actually observe
 - Those that really did receive FDK
 - Those that did not receive FDK
- Ask: Are these two groups comparable?
 - Minimize possibility that observed differences are due to confounding
- Strategies to deal with confounding:
 - Multiple Regression
 - Matching
 - Propensity Score Methods





The Propensity Score—Review

 The Propensity Score: Probability that unit is exposed: The probability that the person receives FDK





The Propensity Score--Review

- If probability (aka propensity score) is close to 1
 VERY LIKELY to receive FDK given observed covariates
- If probability (aka propensity score) is close to 0
 - —VERY UNLIKELY to receive FDK given observed covariates
- Use propensity score to make and compare comparable groups





Weight Population to Estimate Treatment Effects

- Analytic Sample: Everyone Eligible to receive FDK:
- Treatment Effects
 - What is the average effect of the FDK among <u>all of the children who</u> <u>could</u> to receive FDK?
 - What is the effect of FDK among <u>the children who ACTUALLY received</u> FDK?
 - What would the effect of the FDK be for <u>those who were eligible to</u> receive it, but (for whatever reason) did not?





Weight Population to Estimate Treatment Effects

- Analytic Sample: Everyone Eligible to receive FDK:
- Treatment Effects
 - What is the average effect of the FDK among <u>all of the children who</u> <u>could</u> to receive FDK? **ATE**
 - What is the effect of FDK among <u>the children who ACTUALLY received</u> FDK? **ATT**
 - What would the effect of the FDK be for <u>those who were eligible to</u> receive it, but (for whatever reason) did not? ATU





Weight Population to Estimate Treatment Effects

- Treatment Effects—What question does each answer...
 Analytic Sample: Target Population for FDK
 - ATE: What is the effect among the target population?
 - ATT: Ok, we did not reach everyone in our target population... what is the effect among those that we *did* reach?
 - ATU: Ok, we did not reach everyone in our target population... what would the effect have been among those that we *did not* reach?



Treatment Effects: What are the comparison groups?

– Average Treatment Effect for FDK:

We take EVERYONE in the TARGET POPULATION...

- Imagine if EVERY CHILD <u>receives</u> FDK COMPARED WITH...
- Imagine if EVERY CHILD does not receive FDK





Treatment Effects: What are the comparison groups?

– Average Treatment Effect Among the Treated

Limit analyses to dyads WHO LOOK LIKE the dyads that ACTUALLY RECEIVED the benefit

- EVERYONE who <u>actually received</u> FDK COMPARED WITH
- EVERYONE who looks like those who received FDK but did not





Treatment Effects: What are the comparison groups?

– Average Treatment Effect Among the Untreated for FDK

Limit analyses to childrens WHO LOOK LIKE children that ACTUALLY DID NOT RECEIVE FDK

- EVERYONE who <u>actually did not receive</u> FDK COMPARED WITH
- EVERYONE who looks like those who did not receive FDK but actually did





Weights- Setting Up the Weights

Let

- FDK represent indicator for receiving Healthy Baby Benefit:
 - FDK=1 Person <u>ACTUALLY RECEIVED</u> FDK
 - FDK=0 Person <u>ACTUALLY DID NOT RECEIVE</u> FDK
- PS represent propensity score (probability of receiving FDK):
 - PS ranges between 0 and 1
 - PS close to 0 Based on observed covariates, dyad LOOKS LIKE they DID NOT receive FDK
 - PS close to 1 Based on observed covariates, dyad LOOKS LIKE they DID receive FDK





Weights: ATE

Average Treatment Effect :

Imagine we take EVERYONE in the TARGET POPULATION...

- EVERYONE <u>receives</u> FDK
 COMPARED WITH...
- EVERYONE does not receive FDK

WEIGHT_{Average Treatment Effect} = FDK
$$*\frac{1}{PS} + (1 - FDK) * \frac{1}{1 - PS}$$



Weights: ATT

Average Treatment Effect Among the Treated

Limit analyses to dyads WHO LOOK LIKE the dyads that ACTUALLY RECEIVED the benefit

- EVERYONE who <u>actually received</u> FDK
 COMPARED WITH
- EVERYONE who looks like those who received FDK but did not

$$ATT = FDK + (1 - FDK) * \frac{PS}{1 - PS}$$





Weights: ATU

Average Treatment Effect Among the Untreated for FDK

Limit analyses to children WHO LOOK LIKE children that ACTUALLY DID NOT RECEIVE FDK

- EVERYONE who <u>actually did not receive</u> FDK COMPARED WITH
- EVERYONE who looks like children who did not receive FDK but actually did

$$ATU = FDK * \frac{1 - PS}{PS} + (1 - FDK)$$





Articles for More Information

- Hirano K, Imbens G. Estimation of Causal Effects using Propensity Score Weighting: An Application to Data on Right Heart Catheterization. 2001.
- Hirano K, Imbens G. Efficient Estimation of Average Treatment Effects Using the Estimated Propensity Score. 2003.
- McCaffrey D, Ridgeway G, Morral AR. Propensity Score Estimation with Boosted Regression for Causal Effects in Observational Studies. 2004.



